# Novel Garnet-Structure  $Ca<sub>2</sub>GdZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup> Phosphor and Its$ Structural Tuning of Optical Properties

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## **S** Supporting Information

[ABSTRACT:](#page-7-0) Aluminate garnet phosphors  $Ca_2GdZr_2(AlO_4)_3:Ce^{3+}$  (CGZA: $Ce^{3+}$ ) for solid-state white lighting sources are reported. The crystal structure and Mulliken bonding population of the CGZA:Ce<sup>3+</sup> have been analyzed. The larger 5d  $(^{2}D)$  barycenter shift  $\varepsilon_{\rm c}$  and smaller phenomenological parameter  $10D<sub>a</sub>$  of Ce<sup>3+</sup> in CGZA are related to the larger covalent character of Ce−O. The tuning spectral properties of the Ce<sup>3+</sup>doped CGZA-based isostructural phosphors are presented. The splitting of cubic crystal field energy level  ${}^{2}E_{\sigma}$  in  $Ca<sub>2</sub>REZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup> (CREZA:Ce<sup>3+</sup>) (RE = Lu, Y, and Gd)$ increases as the radius of  $\text{RE}^{3+}$  increases, and the splitting of  ${}^{2}\text{E}_{\text{g}}$ may dominate the difference of spectroscopic red-shift  $D(A)$  in



CREZA:Ce<sup>3+</sup>. The splitting of the <sup>2</sup>E<sub>g</sub> in CaGd<sub>2</sub>ZrSc(AlO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup> (CGZSA:Ce<sup>3+</sup>) phosphors increases seemly due to the decreasing of the covalent character of Ce−O. Thermal quenching properties of Ce<sup>3+</sup>-doped CGZA-based isostructural phosphors are also presented and analyzed. For CREZA:Ce $^{3+}$  phosphors, the increasing of the radius of RE $^{3+}$  results in an enhancement of thermal quenching. The quenching of CGZSA: $Ce^{3+}$  is obviously stronger mainly due to the smaller energy difference between the lowest 5d excited state and 4f ground state.

## 1. INTRODUCTION

Phosphor-converted white light emitting diode (pc-WLED) is regarded as one of the most promising eco-friendly light sources.<sup>1,2</sup> The  $Ce^{3+}$  as an activator for phosphor has the lowest 5d state among the trivalent rare earth ions, and the broad absorpt[ion](#page-7-0) and emission bands from the allowed 4f↔5d transitions can even shift from ultraviolet to visible wavelength in some host, especially in garnet crystals. $3,4$ 

It is well-known that garnets with formula unit of  $L_3D_2(AO_4)$ <sub>3</sub> belong to the *Ia* $\overline{3}d$  space gr[oup](#page-7-0). There are three different crystallographic sites for the cations in the  $L_3D_2(AO_4)_3$ , L sites with eight-coordinate in dodecahedron, D sites with six-coordinate in octahedron, and A sites with fourcoordinate in tetrahedron.<sup>5</sup> Ce<sup>3+</sup>-doped garnets have been developed as green, yellow, and even red phosphors via L, D, and A chemical substitutio[ns](#page-7-0) with different ions.<sup>6−8</sup> YAG:Ce<sup>3+</sup> is the most frequently used yellow phosphor after it was reported in 1967 by Balsse and Bril.<sup>7</sup> Ca<sub>3</sub>Sc<sub>2</sub>(SiO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup> and Lu<sub>2</sub>CaMg<sub>2</sub>(SiO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup> garnets also have been developed as green and yellow-orange phospho[rs,](#page-7-0) respectively, in recent years.<sup>6,8</sup>

In this work, a series of  $Ce^{3+}$ -doped isostructural aluminate garn[et](#page-7-0) phosphors containing zirconium, such as  $Ca<sub>2</sub>REZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup> (RE = Lu, Y, and Gd)$  and  $CaGd<sub>2</sub>ZrSc (AIO<sub>4</sub>)<sub>3</sub>: Ce<sup>3+</sup>, have been synthesized by the solid-state reaction$ method. The structure of the representative compound  $Ca_2GdZr_2(AIO_4)$ <sub>3</sub> (CGZA) has been determined to understand the detailed ions distribution in these garnet crystals. The Mulliken bonding population of the  $CGZA:Ce^{3+}$  also has been calculated by density functional theory (DFT) to evaluate the bond character of Ce−O. The photoluminescence properties of these  $Ce^{3+}$  doped CGZA-based isostructural phosphors are presented and analyzed on the basis of the crystal structure and bond character of Ce−O.

## 2. EXPERIMENTAL PROCEDURE

A series of powder samples of  $Ce<sup>3+</sup>$ -doped aluminate phosphors listed in Table 1 were prepared using the solid-state reaction method from  $CaCO<sub>3</sub>$  (AR), SrCO<sub>3</sub> (AR), BaCO<sub>3</sub> (AR), La<sub>2</sub>O<sub>3</sub> (99.99%), Gd<sub>2</sub>O<sub>3</sub> (99.99%), Lu<sub>2</sub>O<sub>3</sub> (99.99%), Y<sub>2</sub>O<sub>3</sub> (99.99%), Sc<sub>2</sub>O<sub>3</sub> (99.99%), ZrO<sub>2</sub>  $(AR)$ ,  $Al_2O_3$   $(AR)$ , and  $CeO_2$   $(99.99%)$  according to the stoichiometric ratio of each sample. The powder reagents were ground together and heated at about 1500−1600 °C for 6−8 h under a reducing atmosphere of  $H_2/N_2$  (5%/95%). The small single crystal of CGZA for structure analysis was obtained by keeping the powder reagents at 1600 °C for 5 days. The X-ray powder diffraction (XRD) data of the samples were obtained by a Rigaku MiniFlex II X-ray diffractometer over an angular range of  $5^{\circ} \le 2\theta \le 80^{\circ}$  with a step size of 0.03°. The crystal structure of CGZA was determined by a Rigaku mercury 70 CCD diffractometer equipped with a graphite-mono-

Received: January 26, 2014 Published: June 10, 2014

<span id="page-1-0"></span>Table 1. List of Sample Compositions

sample	compositions	phase
$CGZA:Ce^{3+}$	$Ca_2Gd_{1-x}Zr_2(AlO_4)_3:xCe^{3+}$ (x = 0.01, 0.02, 0.04, 0.12)	garnet
$CLuZA:Ce3+$	$Ca2Lu0.98Zr2(AlO4)3:0.02Ce3+$	garnet
$CYZA:Ce^{3+}$	$Ca2Y0.98Zr2(AlO4)3:0.02Ce3+$	garnet
$CLaZA:Ce^{3+}$	$Ca2La0.98Zr2(AlO4)3:0.02Ce3+$	mixed
$CSGZA:Ce^{3+}$	$CaSrGd_{0.98}Zr_2(AlO_4)_3:0.02Ce^{3+}$	mixed
$CBGZA:Ce^{3+}$	$CaBaGd_{0.98}Zr_2(AlO_4)_3:0.02Ce^{3+}$	mixed
$CGZSA:Ce3+$	$CaGd_{1.98}ZrSc(AlO4)3:0.02Ce3+$	garnet

chromated Mo K $\alpha$  radiation ( $\lambda = 0.71073$  Å) at 293 K. The measured intensities were corrected for Lorentz and polarization factors. The absorption corrections were performed using the multiscan method. The structure was solved by the direct methods with SHELXS-97<sup>9</sup> and refined by full-matrix least-squares fitting on  $\mathit{F}^{2}$  by SHELX-97.10 Photoluminescence (PL) and photoluminescence excitation ([P](#page-7-0)LE) spectra of the powder phosphors were measured using a Cary Eclip[se](#page-7-0) fluorescence spectrometer at room temperature. The temperaturedependent luminescent spectra were measured using a spectrometer (FL920, Edinburgh) equipped with a homemade heating cell under the excitation of a xenon lamp. The photoluminescence quantum yields of the samples in the visible region (400−800 nm) were measured using a BaSO4 coated integrating sphere in the FLS920 spectrometer.

The Mulliken bonding population analyses $^{11}$  of CGZA: $Ce^{3+}$  as well as GdAG:Ce<sup>3+</sup> for comparison were achieved by using the CASTEP code,<sup>12,13</sup> which relies on a plane-wave-based [D](#page-7-0)FT approach. Electron correlation effects were modeled using the Perdew−Burke−Ernzerhof (PB[E\) ge](#page-7-0)neralized gradient approximation (GGA). Core electrons were replaced by norm-conserving pseudopotentials. For geometry optimizations, a plane wave with cutoff energy of 330 eV was employed. Convergence tolerance thresholds values were set to 2 ×  $10^{-6}$  eV/atom for the total energy,  $5 \times 10^{-2}$  eV/Å for the maximum ionic force, and  $2 \times 10^{-3}$  Å for the maximum ionic displacement. The special points sampling integration over the Brillouin zone was employed by using the Monkhorst−Pack (MP) method with 1 × 1 × 1 special k-point meshes.

## 3. RESULTS AND DISCUSSION

3.1. Phase Formation of Aluminate Garnet Containing Zirconium. The powder X-ray diffraction patterns of the obtained aluminate phosphors containing zirconium as well as the simulated XRD patterns of YAG from the crystal structure  $data<sup>6</sup>$  for comparison are shown in Figure 1. It can be found that the compounds CGZA,  $Ca<sub>2</sub>YZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>$  (CYZA),  $Ca<sub>2</sub>LuZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>$  $Ca<sub>2</sub>LuZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>$  $Ca<sub>2</sub>LuZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>$  (CLuZA), and CaGd<sub>2</sub>ZrSc(AlO<sub>4</sub>)<sub>3</sub> (CGZSA) are isostructural with YAG and can be indexed to the cubic system with space group  $Ia\overline{3}d$  (SG 230), but many impurity phases exist in the  $CaSrGdZr_2(AIO_4)_3$  (CSGZA),  $CaBaGdZr_2(AIO_4)_3$  (CBGZA), and  $Ca_2LaZr_2(AIO_4)_3$ (CLaZA). Generally, the stability of the garnet structure depends upon the radii of the contained cations. For example, the garnets  $RE_3Al_2(AlO_4)_3$  (RE = Gd–Lu, Y) are thermodynamically stable for the rare-earth ions smaller than  $Gd^{3+}$ , but those that contain ions larger than  $Gd^{3+}$   $(La^{3+}-Eu^{3+})$  are not.<sup>14−16</sup> In this work, Ca<sup>2+</sup>, which is larger than Gd<sup>3+</sup>, has been introduced into the L sites of garnet structure with  $Zr^{4+}$  larger than  $Al^{3+}$  $Al^{3+}$  $Al^{3+}$  introduced to the D sites. Furthermore, the cations  $Zr^{4+}$  at D sites can also be substituted by  $Sc^{3+}$  with similar radius partly to form the CGZSA compound, and the garnet lattices are still stable. However, further expansion of the host lattice by introducing cations such as  $La^{3+}$ ,  $Sr^{2+}$ , and  $Ba^{2+}$  larger than  $Ca^{2+}$  to the L sites destabilizes formation of the garnet containing zirconium.



Figure 1. X-ray powder diffraction patterns of the aluminate phosphors containing zirconium and YAG.

3.2. Structure Characteristics of CGZA. To understand the detailed ion distribution in the garnet crystal, the structure of CGZA crystal was analyzed as a representative compound. The diffraction data of CGZA crystal can be indexed to the cubic system. For the final acceptable refinement, which relates to a lower R factor, the  $Al^{3+}$  ions occupy the A sites, the larger  $Zr^{4+}$  ions occupy the D sites, and the largest  $Ca^{2+}$  and  $Gd^{3+}$  ions occupy the L sites with a ratio of 2:1. The simulated XRD patterns of CGZA from the crystal structure data are also given in Figure 1 for comparison. The crystallographic data and structure refinement for the CGZA crystal are listed in Table 2. The atomic coordinates and isotropic thermal parameters are listed in Table 3.

Figure 2a displays the central projection (perspective) of [a](#page-2-0) unit cell of C[GZ](#page-2-0)A crystal along the (001) axis. The 24c, 16a, and 24d Wyckoff sites are fully occupied by  $Ca^{2+}/Gd^{3+}$ ,  $Zr^{4+}$ , and  $Al^{3+}$ , [r](#page-3-0)espectively. The  $AlO_4$  tetrahedrons, which link the cations between them, are isolated from each other. Every Ca/ Gd is surrounded by four  $(Ca/Gd)O_8$ , four  $ZrO_6$ , and six AlO<sub>4</sub> polyhedrons, which means that every coordination  $O^{2-}$  anion of Ca/Gd is shared by four cations, one  ${\rm Zr^{4+}}$ , one  ${\rm Al}^{3+}$ , and two  $Ca^{2+}/Gd^{3+}$ , as shown in Figure 2b.

The selected interatomic distances and the values of bond valence sum  $(BVS)^{17}$  of CGZA [ar](#page-3-0)e listed in Table 4. In CGZA crystal, the bond valence for  $Gd^{3+}$  ions is lower than the normal value of 3, but for  $Ca^{2+}$  it is slightly higher [t](#page-3-0)han the normal value of 2. It is known that bond valences are associated with bond distances. Higher or lower bond valence means that the space occupied by an ion is smaller or larger than the normal space for it. Considering the radius of  $Ca^{2+}$  is larger than that of  $Gd^{3+}$  and the bond distances obtained from X-ray diffraction are average values, the departure of bond valences from the

<span id="page-2-0"></span>Table 2. Crystallographic Data and Structure Refinement for CGZA

empirical formula	$Ca2GdZr2(AlO4)3$
formula wt	692.79
temp(K)	293(2)
wavelength (Å	0.71073
crystal system	cubic
space group	$Ia\overline{3}d$
unit cell dimensions (A)	$a = 12.5057(7)$
volume $(A^3)$	1955.88(19)
Z	8
calcd density $(g/cm3)$	4.706
abs coeff $(mm^{-1})$	10.184
F(000)	2552
crystal size (mm)	$0.2 \times 0.1 \times 0.05$
$\theta$ range for data collection (deg)	$3.99 - 27.5$
limiting indices	$-16 \le h \le 15, -16 \le k \le 15, -16 \le l \le 15$
reflns collected/unique	6371/192 $[R_{\text{int}} = 0.0431]$
completeness to $\theta = 27.47^{\circ}$	100%
max and min transmission	1.0000 and 0.5992
abs correction	none
refinement method	full-matrix least-squares on $F^2$
data/restraints/ parameters	192/0/19
GOF on $F^2$	1.164
final R indices $[I > 2\sigma(I)]$	$R_1 = 0.0162$ , $wR_2 = 0.0417$
R indices (all data)	$R_1 = 0.0162$ , w $R_2 = 0.0417$
extinction coeff	0.00087(7)
largest diff. peak and hole	0.309 and $-0.400 \text{ e} \text{ Å}^{-3}$

normal values for both  $Ca^{2+}$  and  $Gd^{3+}$  also indicates that  $Ca^{2+}$ and  $Gd^{3+}$  occupy L sites simultaneously to some extent. The BVS of  $Al^{3+}$  cation at A site in CGZA is lower than the normal value of 3, which means that the Al−O bond length in the crystal is longer slightly than that in a usual compound containing  $[AlO<sub>4</sub>]^{5-}$  group, such as  $Sr<sub>2</sub>EuAlO<sub>5</sub>$  (BVS = 3.003).<sup>18</sup> The BVS values of  $Zr^{4+}$  ion at D sites are close to the normal value of 4. The selected bond angles of CGZA and REAG [\(](#page-7-0)RE = Y, Gd) crystals are listed in Table 5 for comparison. It is worth noting that the  $\alpha$ ,  $\beta$ , and  $\delta$  in LO<sub>8</sub> dodecahedron as shown in Figure 2c are different in orde[r,](#page-3-0) that is,  $\alpha < \beta < \delta$  in CGZA but  $\beta < \alpha < \delta$  in REAG. That is, the shapes of  $LO_8$  dodecahedron in [t](#page-3-0)he CGZA and REAG are different.

3.3. Chemical Bond Characteristics. The covalency between the anion ligands and  $Ce^{3+}$  ion would not only reduce energy level splitting of d electrons caused by the crystal field, spin−orbit interaction, and Jahn−Teller coupling effect, but

also shift down the barycenter of 5d  $(^{2}D)$  states.<sup>19–22</sup> The covalent character of Ce−O bonds in garnets is affected by the cations at L, D, and A sites because the  $O^{2-}$  anion [conn](#page-7-0)ected with  $Ce^{3+}$  is also shared by the other three cations. Increasing the electronegativety of cations at L, D, and A sites may decrease the covalent character of Ce−O bonds in Ce3+-doped garnets. However, it is difficult to make a prediction about the changing trend of covalent character of Ce−O bonds in CREZA: $Ce^{3+}$  (RE = Lu, Y, and Gd) from that in REAG: $Ce^{3+}$ because the average electronegativity of cations at L sites is decreased due to the  $RE^{3+}$  substituted by  $Ca^{2+}/RE^{3+}$ , but the electronegativity of cations at D sites is increased due to the  $Al^{3+}$  substituted by  $Zr^{4+}$ . Therefore, the Mulliken bonding population analyses of  $CGZA:Ce^{3+}$  as well as  $GdAG:Ce^{3+}$  for comparison have been performed by DFT to evaluate the covalent character of Ce−O bond in both garnets. The supercell models used in the DFT calculation are shown in Figure 3. The nominal formulas for the supercell models are  $Ca_2Gd_{0.75}Ce_{0.25}Zr_2(AIO_4)$ <sub>3</sub> and  $Gd_{2.75}Ce_{0.25}Al_2(AIO_4)$ <sub>3</sub>, respectively. [Th](#page-4-0)e calculated values of the Mulliken bond population and bond length are listed in Table 6. It is worth noting that the covalent character of Ce−O bond in CGZA:Ce3+ is larger than that in GdAG: $Ce^{3+}$ ; even the  $Zr^{4+}$  [w](#page-4-0)ith larger electronegativity has been introduced to D site, and which indicates that the  $Ca<sup>2+</sup>$  with smaller electronegativity at L site dominates the covalent character of Ce−O bonds in CGZA:Ce3+. Consequently, the combined effect of  $RE<sup>3+</sup>$  being substituted by  $Ca^{2+}/RE^{3+}$  and  $Al^{3+}$  being substituted by  $Zr^{4+}$  to form CREZA from REAG increases the covalent character of the Ce−O bond in CREZA.

**3.4. Spectral Property of CGZA:Ce<sup>3+</sup>.** Figure 4 shows the energy level scheme for  $Ce^{3+}$  in garnet. The barycenter of 5d  $({}^{2}D)$  state as a free ion would shift down to the  $T<sub>d</sub>$  [po](#page-4-0)sition due to the nephelauxetic effect<sup>19,20,22</sup> closely related to the covalency between  $Ce^{3+}$  and  $O^{2-}$  ligands. The splitting of the 5d (<sup>2</sup>D) state in garnets can [be rel](#page-7-0)ated to a  ${}^{2}T_{2g} - {}^{2}E_{g}$  cubic crystal field splitting with the additional splitting due to the distortion of the cubic coordination into a dodecahedron with  $D_2$  symmetry.<sup>23</sup> In general, the absorption in Ce<sup>3+</sup>-doped garnet phosphor is caused by the transitions from the  ${}^{2}F_{5/2}$  multiplet of 4f configur[ati](#page-7-0)on to the five energy levels of 5d  $\left(\frac{2D}{D}\right)$  state, and the visible light emission is related to the transitions from the lowest-lying level <sup>2</sup> $A_{1g}$  to the <sup>2</sup> $F_{7/2}$  and <sup>2</sup> $F_{5/2}$  multiplets.<sup>24–26</sup> Figure 5c shows the normalized PL and PLE spectra of the  $CGZA:0.02Ce<sup>3+</sup>$  garnet phosphor. The broad lumines[cence](#page-7-0) band o[f C](#page-4-0)GZA:Ce<sup>3+</sup> with peak wavelength of 500 nm exhibits the potential as a useful green phosphor for general lighting. The asymmetric emission band is fitted as a sum of two components using a Gaussian least-squares fitting, and the splitting between the  ${}^{2}F_{7/2}$  and  ${}^{2}F_{5/2}$  multiplets is estimated to be 1973 cm<sup>-1</sup>. Two bands corresponding to excitations from  ${}^{2}F_1$  equals to the two lowest lying levels  ${}^{2}A$  and  ${}^{2}B$  of 5d  $F_{5/2}$  multiple to the two lowest-lying levels  ${}^{2}A_{1g}$  and  ${}^{2}B_{1g}$  of 5d

Table 3. Atomic Coordinates and Isotropic Thermal Parameters for CGZA

atom	Wyck.	$\boldsymbol{\mathcal{X}}$		$\boldsymbol{z}$	SOF	$U_{\rm eq}^{\phantom{1}a}$
Zr	16a	0.25	0.75	0.25		0.0005(1)
Gd	24c	0.25	0.625	$\mathbf{0}$	1/3	0.0007(1)
Ca	24c	0.25	0.625	0	2/3	0.0007(1)
Al	24d	0.25	0.375	0		0.0004(1)
O	96h	0.3453(2)	0.4666(2)	0.0523(2)		0.0008(1)

 ${}^aU_{\text{eq}}$  is defined as one-third of the trace of the orthogonalized  $U_{ij}$  tensor.

<span id="page-3-0"></span>







Figure 2. (a) Unit-cell representation of  $Ca_2GdZr_2(AIO_4)_{3}$ ; (b) coordination geometry of Ca/Gd in Ca<sub>2</sub>GdZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>; and (c) LO<sub>8</sub> dodecahedron,  $AO_4$  tetrahedron, and  $DO_6$  octahedron, and the selected bond angles in  $Ca<sub>2</sub>GdZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>$ .

( 2 D) can be distinguished from the PLE spectrum of the CGZA:0.02Ce<sup>3+</sup>. The splitting of the <sup>2</sup>E<sub>g</sub> can be estimated as 5345 cm<sup>-1</sup>, and the barycenter of <sup>2</sup>E<sub>g</sub> is determined as 26 650 cm<sup>-1</sup>. Furthermore, the position of  ${}^{2}$ A<sub>1g</sub> can be determined as 23 980 cm<sup>-1</sup>, and thus the spectroscopic red-shift  $D(A)^{27}$ relative to the centroid position 51 230 cm $^{-1}$  of 5d (<sup>2</sup>D) state of Ce3+ as a free ion is about 25 360 cm<sup>−</sup><sup>1</sup> . Comparing t[he](#page-7-0)

## Table 4. Selected Bond Lengths (Å) and Bond Valence Sums (BVS) for  $CGZA^a$



"Symmetry transformations used to generate equivalent atoms:  $(\#1)$  y  $-1/4$ ,  $x + 1/4$ ,  $-z + 1/4$ ,  $(2x + 1/4, z + 3/4, y - 1/4, (2x + 3/4, z + 3/4))$  $3/4$ ,  $-z + 3/4$ ,  $-y + 3/4$ ,  $($ #4 $) -z + 1/4$ ,  $y + 1/4$ ,  $-x + 3/4$ ,  $($ #5 $) z +$  $1/4$ ,  $-y + 5/4$ ,  $x - 1/4$ ,  $(#6) -y + 3/4$ ,  $-x + 5/4$ ,  $z + 1/4$ ,  $(#7) -x +$  $1/2$ ,  $-y + 3/2$ ,  $-z + 1/2$ ,  $(#8) z + 1/2$ ,  $x + 1/2$ ,  $y - 1/2$ ,  $(#9) -y + 1$ ,  $z + 1/2$ ,  $-x + 1/2$ ,  $(\#10) -x + 1/2$ ,  $y + 0$ ,  $-z + 0$ ,  $(\#11) -z + 1/4$ ,  $-y$ +  $5/4$ ,  $-x$  +  $1/4$ ,  $(#12)$   $-y$  +  $3/4$ ,  $x$  +  $1/4$ ,  $z$  -  $1/4$ ,  $(#13)$   $-z$  +  $1/2$ ,  $-x + 1$ ,  $y - 1/2$ ,  $(#14)$   $z + 0$ ,  $-x + 1$ ,  $-y + 1/2$ ,  $(#15)$   $x$ ,  $y + 1/2$ ,  $-z$ ,  $(\text{\#16}) \ z + 1/4, -y + 3/4, -x + 1/4, (\text{\#17}) - z + 1/4, -y + 3/4, x - 1/4)$ 4,  $(\#18)$  x,  $y - 1/2$ ,  $-z$ .

Table 5. Selected Angles (deg) of CGZA, YAG, and GdAG Crystals

polyhedron	angle	YAG <sup>5</sup>	GdAG <sup>5</sup>	CGZA
dodecahedron	$\alpha$ (O-L-O)	71.833	71.850	68.889
	$\beta$ (O-L-O)	67.905	67.802	71.470
	$\delta$ (O-L-O)	73.575	74.066	72.251
octahedron	$\varphi$ (O-D-O)	86.633	86.957	87.615
	$\rho$ (O-A-O)	93.367	93.043	92.385
tetrahedron	$\gamma$ (O-A-O)	99.981	100.599	99.825
	$\theta$ (O-D-O)	114.415	114.081	114.499

absorption and emission bands originating from the transitions between  ${}^{2}F_{5/2}$  and  ${}^{2}A_{1g}$ , the Stokes shift  $E_{s}$  of  ${}^{2}A_{1g}$  in CGZA:Ce3+ can be determined to be 3489 cm<sup>−</sup><sup>1</sup> . The 5d (<sup>2</sup>D) barycenter shift  $\varepsilon_c$  of Ce<sup>3+</sup> in CGZA can be estimated by the following expression:27−<sup>30</sup>

$$
\varepsilon_{\rm c} = 1.79 \times 10^{13} \sum_{i=1}^{N} \frac{\alpha_{\rm sp}^i}{\left(R_i - 0.6\Delta R\right)^6} \tag{1}
$$

$$
\alpha_{\rm sp} = 0.33 + \frac{4.8}{\chi_{\rm av}^2} \tag{2}
$$

<span id="page-4-0"></span>

Figure 3. Supercell models for (a)  $Ca_2GdZr_2(AIO_4)_3:Ce^{3+}$  and (b)  $Gd_3Al_5O_{12}:Ce^{3+}$ .







Figure 4. Energy level scheme for  $Ce^{3+}$  in garnet.

$$
\chi_{\text{av}} = \frac{\sum_{i} n_{i} z_{i} \chi_{i}}{\sum_{i} n_{i} z_{i}} \tag{3}
$$

where  $R_i$  is the Ce<sup>3+</sup>−anion distance in the undistorted lattice, N represents the number of anions coordinated to  $Ce^{3+}$ ,  $\Delta R$  is the difference in ionic radii for the cation at L site and  $Ce^{3+}$ ,  $\chi_{av}$ is the weighted average of the cation electronegativity in a given oxide host lattice,  $n_i$  is the number of cations of type  $i$  with charge  $+z_i$ , and  $\chi_i$  is Pauling type electronegativity values.<sup>31</sup> The 5d (<sup>2</sup>D) barycenter shift  $\varepsilon_{\rm c}$  of Ce<sup>3+</sup> in CGZA is estimated as 17



Figure 5. Normalized PL and PLE spectra of (a)  $Ca<sub>2</sub>LuZr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup>;$  (b)  $Ca<sub>2</sub>YZr(AlO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup>;$  (c)  $Ca_2GdZr_2(AIO_4)_3:Ce^{3+}$ ; and (d)  $CaGd_2ZrSc(AIO_4)_3:Ce^{3+}$ .

380 cm<sup>−</sup><sup>1</sup> , which is larger than that of the typical garnets YAG:Ce<sup>3+</sup> (14 250 cm<sup>-1</sup>) and GdAG:Ce<sup>3+</sup> ( $\varepsilon_c = 14 \text{ } 160 \text{ cm}^{-1}$ ). The T<sub>d</sub> position thus can be estimated as 33 850 cm<sup>-1</sup> relative to the centroid position 51 230 cm<sup>-1</sup> of 5d (<sup>2</sup>D) state of Ce<sup>3+</sup> as a free ion. The energy difference between the barycenters of  ${}^2\mathrm{E_g}$ and  $T<sub>d</sub>$  is about 1.5 times the energy difference between the barycenters of <sup>2</sup>T<sub>2g</sub> and T<sub>d</sub> in cubic coordination;<sup>32</sup> that is, T<sub>d</sub> –<br><sup>2</sup>E – 1 S(<sup>2</sup>T – T<sub>c</sub>) and the barycenter of <sup>2</sup>T<sub>c</sub> therefore can  $E_{g} = 1.5(^{2}T_{2g} - \tilde{T}_{d})$ , and the barycenter of  $^{2}T_{2g}$  therefore can be calculated as 38 650  $cm^{-1}$  and thus the splitti[ng](#page-7-0) between the  $T_{2g}$  and  ${}^{2}E_{g}$  levels represented by the phenomenological parameter  $10D_q$  is determined as 12 000 cm<sup>-1</sup>. The  $10D_q$  of CGZA:Ce<sup>3+</sup> is smaller than that of GdAG:Ce<sup>3+</sup> (19 080 cm<sup>-1</sup>). The larger  $\varepsilon_c$  and smaller 10D<sub>q</sub> of Ce<sup>3+</sup> in CGZA than those in GdAG, respectively, are related to the larger covalent character of Ce−O in CGZA as discussed in section 3.3.

Figure 6 shows the normalized PL spectra of CGZA: $xCe^{3+}$ with  $x = 0.01 - 0.12$  under excitation at 415 [nm.](#page-2-0) The peak of PL



Figure 6. Normalized PL spectra for Ca<sub>2</sub>Gd<sub>(1-x)</sub>Zr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>: $xCe^{3+}$  ( $x =$ 0.01, 0.02, 0.04, ...0.12).

band shifts to longer wavelength from 499 nm for  $x = 0.01$  to 514 nm for  $x = 0.12$ . The emission intensity of samples obtained by integrating the relative emission bands for  $CGZA:xCe^{3+}$  ( $x = 0.01$ , 0.02, 0.04, ...0.12) measured at the same condition is shown in Figure 7. It can be found that the maximum emission is at  $x = 0.02$ .



Figure 7. Relative integrated emission intensities for  $Ca_2Gd_{(1-x)}Zr_2(AIO_4)_3:xCe^{3+}$  (x = 0.01, 0.02, 0.04, ...0.12).

3.5. Tuning Spectral Properties of Ce<sup>3+</sup>-Doped CGZA-Based Isostructural Phosphors. The emission color of Ce<sup>3+</sup>doped phosphors can be tuned by adjusting the composition of host or codoping the other activators.<sup>33,34</sup> Figure 5a, b, d shows a series of the PL and PLE spectra of CGZA-based isostructural garnet phosphors studied in this wo[rk. T](#page-7-0)he em[iss](#page-4-0)ion color of these phosphors as shown in Figure 8 could be tuned from blue (peak at 480 nm with CIE chromaticity coordinate at  $(x = 0.16,$ 



Figure 8. CIE coordinates of  $Ca_2Lu_{0.98}Zr_2(AIO_4)_3:0.02Ce^{3+}$  $Ca_2Y_{0.98}Zr_2(AlO_4)_3:0.02Ce^{3+}$ ,  $Ca_2Gd_{0.98}Zr_2(AlO_4)_3:0.02Ce^{3+}$ , and  $CaGd_{1.98}ZrSc(AlO<sub>4</sub>)<sub>3</sub>:0.02Ce<sup>3+</sup>.$ 

 $y = 0.27$ ) to green-yellow (peak at 545 nm with CIE chromaticity coordinate at  $(x = 0.39, y = 0.54)$  with the L and D sites occupied by  $Lu^{3+}$ ,  $Y^{3+}$ ,  $Gd^{3+}$ , and  $Sc^{3+}$ , respectively. The emission peak wavelength, 5d  $(^{2}D)$  barycenter shift  $\varepsilon_c$ , phenomenological parameter  $10D_{\rm q}$ , splitting of  $^2{\rm E}_{{\rm g}^2}$  the barycenter of  ${^2\mathrm{E}}_{\mathrm{g}l}$  spectroscopic red-shift  $D(A)$ , and the  $\mathrm{\mathring{S}}$ tokes shift  $E_s$  of the Ce<sup>3+</sup>-doped CGZA-based isostructural phosphors as well as  $REAG:Ce^{3+}$  (RE = Lu, Y, and Gd) phosphors for comparison are summarized in Table 7.

The 5d (<sup>2</sup>D) barycenter shifts  $\varepsilon_c$  and phenomenological parameters  $10D_{q}$  of  $Ce^{3+}$  in REA[G](#page-6-0): $Ce^{3+}$  are very close, respectively, which may be due to the similar electronegativity of RE<sup>3+</sup>. This result also allows one to deduce that the  $\varepsilon_c$  and  $10D<sub>a</sub>$  of Ce<sup>3+</sup> in CREZA:Ce<sup>3+</sup> are also similar and are about 17 400 and 12 000 cm<sup>−</sup><sup>1</sup> , respectively.

In garnet, the  ${}^{2}E_{g}$  of  $Ce^{3+}$  is not degenerated in the crystal field of  $D_2$  point symmetry, and it is not necessary to consider the typical Jahn–Teller effect, but the  $E_g \times e_g$  Jahn–Teller mode as a coupling still strongly influences the splitting of  ${}^{2}E_{\text{g}}$ . With larger cation occupying the L sites in the garnet, the tetragonal distortions of  $CeO_8$  (LO<sub>8</sub>) cube, which is related to the symmetric bending of Ce−O(L−O) bonds with the e<sub>e</sub> $\theta$ irreducible representation, would be enhanced.<sup>21,39−43</sup> Therefore, the splitting of  ${}^{2}E_{g}$  would be increased with the radius of L ion obviously due to the Jahn-Teller couplin[g e](#page-7-0)[ff](#page-7-0)e[ct.](#page-7-0)<sup>39,40</sup> As expected, the splitting of <sup>2</sup>E<sub>g</sub> in CREZA:Ce<sup>3+</sup> (RE = Lu, Y, and  $Gd)$  increases with the radius of  $RE<sup>3+</sup>$  ion, which is si[milar](#page-7-0) to that in REAG:Ce<sup>3+</sup> phosphors. It is also worth noting that the splittings of  ${}^{2}E_{g}$  in CREZA:Ce<sup>3+</sup> garnet phosphors are smaller than those in  $REAG:Ce<sup>3+</sup>$  garnet phosphors, which may be mainly due to the larger covalent character of Ce−O in CREZA: $Ce^{3+}$  and the difference in the shapes of  $CeO_8$  (LO<sub>8</sub>) dodecahedron in these garnets as discussed in section 3.2. Partly substituting the  $Zr^{4+}$  by  $Sc^{3+}$  at the D sites and  $Ca^{2+}$  by  $Gd^{3+}$  at the L sites to form CGZSA: $Ce^{3+}$  phosphors see[mly](#page-1-0) decreases the covalent character of the Ce<sup>3+</sup> and  $O^{2-}$  ligand and

<span id="page-6-0"></span>

thus increases the splitting of the  ${}^{2}E_{g}$  because the distortion of  $CeO_8$  (LO<sub>8</sub>) polyhedrons would be decreased due to the introduction of more  $Gd^{3+}$  ions, which lead to a smaller average cation radius at L sites.

The spectroscopic red-shift  $D(A)$  is determined by the splitting of the 5d  $(2D)$  state and the barycenter shift of 5d  $(2D)$ state as compared to free ion. Because the  $\varepsilon_c$  and  $10D_q$  of Ce<sup>3+</sup> in CREZA: $\text{Ce}^{3+}$  are similar, respectively, the splitting of  ${}^{2}\text{E}_{g}$ may dominate the difference of  $D(A)$  in CREZA:Ce<sup>3+</sup>. Therefore, the  $D(A)$  in CREZA: $Ce^{3+}$  would increases with the radius of  $\text{RE}^{3+}$  as does  ${}^{2}\text{E}_{\text{g}}$ . The larger covalent character of Ce–O in CREZA:Ce<sup>3+</sup> would lower the 5d (<sup>2</sup>D) barycenter but decrease the splitting more due to the crystal field and Jahn− Teller coupling effect existing simultaneously; the spectroscopic red-shift  $\tilde{D}(A)$  in CREZA: $\tilde{C}e^{3+}$  is therefore generally smaller than that in  $REAG:Ce^{3+}$ .

The Stokes shift  $E_s$  is caused by the lattice relaxation.<sup>44</sup> The  $E_s$  increases with the radius of  $RE^{3+}$  in both CREZA:Ce<sup>3+</sup> and REAG: $Ce^{3+}$  due to the increasing of distortion of  $CeO_8$  [\(L](#page-7-0)O<sub>8</sub>) polyhedrons, which leads to the stronger electron−phonon interaction.<sup>45,46</sup>

3.6. Thermal Quenching of Luminescence and Quantum [Yie](#page-7-0)lds of Ce<sup>3+</sup>-Doped CGZA-Based Isostructural Phosphors. Temperature dependence of relative integral emission intensities related to the transitions from the lowestlying level  ${}^2A_{1g}$  to the  ${}^2F_{7/2}$  and  ${}^2F_{5/2}$  multiplets for  $CREZA:Ce^{3+}$  and  $CGZSA:Ce^{3+}$  are shown in Figure 9. The thermal quenching properties of phosphor are related to the active energy barriers  $\Delta E_a^{47-50}$  for nonradiative relaxation processes. Stronger electron−phonon interaction and smaller



Figure 9. Temperature dependence of photoluminescence intensity on  $Ca<sub>2</sub>Lu<sub>0.98</sub>Zr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>:0.02Ce<sup>3+</sup>, Ca<sub>2</sub>Y<sub>0.98</sub>Zr<sub>2</sub>(AlO<sub>4</sub>)<sub>3</sub>:0.02Ce<sup>3+</sup>,$  $Ca_2Gd_{0.98}Zr_2(AlO_4)_3:0.02Ce^{3+}$ , and  $CaGd_{1.98}ZrSc(AlO_4)_3:0.02Ce^{3+}$ phosphors.

energy difference between excited and ground [st](#page-7-0)a[te](#page-7-0) means a lower  $\Delta E_a$  and a stronger nonra[dia](#page-7-0)t[ive](#page-7-0) process.<sup>47-49</sup> For CREZA:Ce3+ phosphors, the luminescence temperature quenching of  $\tilde{Ce}^{3+}$  enhances with the radius of  $RE^{3+}$  [du](#page-7-0)e to the enhancement of electron−phonon interaction caused by the increasing of distortion of  $CeO_8$  (LO<sub>8</sub>) polyhedrons. In fact, the larger distortion of  $CeO_8$   $(LO_8)$  polyhedrons in CGZA-based garnet phosphors caused by introducing larger  $Ca<sup>2+</sup>$  to L-sites of the garnets also leads to that the temperature quenching of Ce<sup>3+</sup>-doped CGZA-based garnet phosphors is more serious than that of REAG:Ce<sup>3+</sup>.<sup>51,52</sup> The quenching of  $CGZSA:Ce^{3+}$  is stronger than that of  $CGZA:Ce^{3+}$ , which indicated that the  $\Delta E_{a}$  of CGZSA:Ce<sup>[3+](#page-7-0)</sup> [de](#page-7-0)creases due to the smaller energy difference between the lowest 5d excited state and 4f ground state.

The quantum yields of CGZA-based phosphors measured at room temperature are given in Table 7 for comparison. The quantum yield is also related to the  $\Delta E_a$ , so it would be lower in the phosphor with stronger luminescence thermal quenching.

## 4. CONCLUSIONS

In this work, a series of  $Ce^{3+}$ -doped aluminate phosphors containing zirconium MREZA: $Ce^{3+}$  (M = Ca, Sr, Ba and RE = La, Gd, Y, Lu) and  $CGZSA:Ce<sup>3+</sup>$  have been synthesized by the solid-state reaction method. The compounds CGZA, CLuZA, CYZA, and CGZSA crystallize in cubic system with space group  $Ia\overline{3}d$ , but many impurity phases exist in CSGZA, CBGZA, and CLaZA. The Mulliken bonding population analyses of the  $CGZA:Ce^{3+}$  as well as  $GdAG:Ce^{3+}$  for comparison show that the covalent character of Ce−O bonds in CGZA:Ce3+ is larger than that in  $GdAG:Ce^{3+}$ . The photoluminescence properties of CGZA: $xCe^{3+}$  (0.01  $\leq x \leq 0.12$ ) were investigated, and the maximum emission occurred at  $x = 0.02$ . The tuning spectral properties of Ce3+-doped CGZA-based isostructural phosphors by substituting the cations with  $Y^{3+}$ ,  $Lu^{3+}$ , and  $Sc^{3+}$  were analyzed. The splitting of <sup>2</sup>E<sub>g</sub> in CREZA:Ce<sup>3+</sup> (RE = Lu, Y, and Gd) increases as the radius of RE<sup>3+</sup> increasing. The  $\varepsilon_c$  and  $10D_q$ of Ce<sup>3+</sup> in CREZA:Ce<sup>3+</sup> are similar, and are about 17 400 and 12 000 cm<sup>-1</sup>, respectively. The splitting of <sup>2</sup>E<sub>g</sub> may dominate the difference of  $D(A)$  in CREZA:Ce<sup>3+</sup>, and the  $D(A)$  in CREZA: $Ce^{3+}$  therefore increases with the radius of  $RE^{3+}$  as does  ${}^{2}E_{g}$ . The splitting of the  ${}^{2}E_{g}$  in CaGd<sub>2</sub>ZrSc(AlO<sub>4</sub>)<sub>3</sub>:Ce<sup>3+</sup>  $(CGZS\AA:Ce^{3+})$  phosphors increases seemly due to the decreasing of the covalent character of the Ce−O. The E<sup>s</sup> also increases with the radius of RE<sup>3+</sup> in both CREZA:Ce<sup>3+</sup> and REAG: $Ce^{3+}$  due to the increasing of distortion of  $LO_8$ polyhedrons. Thermal quenching properties of Ce<sup>3+</sup>-doped CGZA-based isostructural phosphors are analyzed. For CREZA: $Ce^{3+}$  phosphors, the increasing of the radius of  $RE^{3+}$ 

<span id="page-7-0"></span>decreases the active energy barriers for nonradiative relaxation processes and results in a enhancement of thermal quenching. The quenching of  $CGZSA:Ce^{3+}$  is stronger than that of  $CGZA:Ce^{3+}$ , which is mainly due to the smaller energy difference between the lowest 5d excited state and 4f ground state.

## ■ ASSOCIATED CONTENT

#### **S** Supporting Information

CIF data. This material is available free of charge via the Internet at http://pubs.acs.org.

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#### Notes

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#### ■ ACKNOWLEDGMENTS

This work has been supported by the Science and Technology Major Project of Fujian Province (Grant no. 2011HZ0001-2).

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